

# Physics with stopping muons in Daya Bay

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Technical note in doc-2232.

# Introduction

- Roughly 2% and 5% of muons incident on the far and near sites will stop in the water pools, respectively.
- Only consider stopping muons in AD at near sites because flux $\times$ stopping rate is 50 times lower at far site and products of stopped muons create too few PE in water pool.

The possible measurements are

- 1 The cosmic muon charge ratio,
- 2 The neutron multiplicity from  $\mu^-$  C captures, and
- 3 The  $\mu^-$  capture rate on gadolinium.

# Estimate of number of stopped muons/AD/year

- 5% of incident muons stop in water pool
- cosmic muon rate is  $1.2(0.7) \text{ Hz/m}^2$  at the Daya Bay(Ling Ao) near sites
- OAV volume / rectangular pool volume is  $4\pi^2/(16 \times 10 \times 10) \approx 1/10\pi$

$$1\text{Hz/m}^2 \times (16 \times 10\text{m}^2) \times 0.05 \times 1/(10\pi) \times \pi \times 10^7\text{s/yr} \approx 8 \times 10^6/\text{AD/yr} \quad (1)$$

# $\mu^-$ -C capture rate

The cosmic  $\mu^+/\mu^-$  charge ratio is approximately 1.3 and  $\sim 8\%$  of the stopped  $\mu^-$  are captured on carbon, so the number of  $\mu^-$  captures on carbon is

$$8 \times 10^6 \times 1/(1 + 1.3) \times 0.08 \approx 2.8 \times 10^5 \text{ captures/AD/yr} . \quad (2)$$

This is comparable to the sample of  $1.8 \times 10^5 \mu^-$ - $^{12}\text{C}$  captures in a published result on n-emission after  $\mu^-$ -C capture.

We could measure

- 1 neutron multiplicity
- 2 neutron energy (requires inferring energy from distance between muon track endpoint and neutron capture point)

# $\mu^-$ -Gd capture rate

- Rough estimate of relative rate of  $\mu^-$  capture on Gd compared to C with the “Fermi-Teller Z law” which assumes that the capture rate is proportional to  $Z$  and the concentration of Gd.
- Assuming GdLS is 0.1% Gd and 90% C by weight, the relative capture rate is  $0.1/90 \times 64/6 \approx 0.012$ .
- Negative muon captures on Gd can only occur in the inner acrylic volume which is  $(3.10/3.97)^3 = 0.476$  of the OAV so the estimated rate of  $\mu^-$ -Gd captures is

$$2.8 \times 10^5 \mu^- \text{C}/\text{AD}/\text{yr} \times 0.476 \times 0.012 \approx 1600 \mu^- \text{Gd}/\text{AD}/\text{yr} . \quad (3)$$

- This rate could enable a measurement of the Gd concentration to a statistical precision of  $\sim 2.5\%$ .
- The mean lifetime for  $\mu^-$  in Gd nuclei is  $80.6 \pm 0.8$  ns which may be hard to measure with current electronics.

# Cosmic muon charge ratio

The charge ratio  $r$  can be determined from the mean observed lifetime for stopping muons

$$\tau_m = f\tau_- + (1 - f)\tau_+ \quad (4)$$

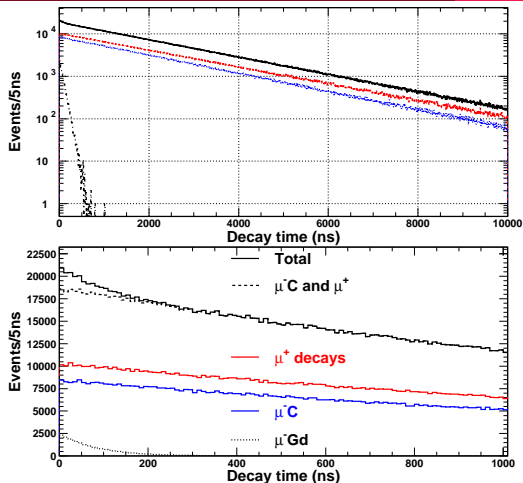
where

- $f = \frac{1}{1+r}$  is the fraction of negative stopped muons,
- $\tau_+ = 2197.03 \pm 0.04$  ns is the  $\mu^+$  lifetime and
- $\tau_- = 2028 \pm 2$  ns is the  $\mu^-$  lifetime in  $^{12}\text{C}$

For a year's exposure of  $N = 8 \times 10^6$  stopped muons in a single AD, the precision on the  $\mu^+/\mu^-$  charge ratio would be  $\sim 0.024$ .

For comparison, recent MINOS measurement:

$$r = 1.270 \pm 0.003(\text{stat}) \pm 0.013(\text{syst})$$



The expected decay time distribution for a background-free, half-year exposure ( $4 \times 10^6$  stopped muons)